# Experimental study on fluid-structure interaction of a flexible membrane wing

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### **Abstract**

A time-resolved particle image velocimetry (PIV) experiment was carried out to investigate the fluid-structure interaction (FSI) of a flexible membrane wing at a moderate angle of attack and low Reynolds numbers. The model was composed of a flexible membrane sheet and rigid leading/trailing edge supports. The dynamic characteristics of the membrane wing was firstly analyzed. While interacting with the fluid, the membrane would perform strongly periodic vibrations and present a shift of vibration modes with the increase of Reynolds number. The flow field was also captured in this study. It was found that the fluid-structure interaction played an important role in affecting the vortex shedding process over the wing surface.

## 1 Introduction

With the development of aviation, micro air vehicles (MAVs) are being applied for increasing purposes. As Shyy et al. (2005) indicated, MAVs have three prominent features: low Reynolds number ( $10^4 \sim 10^5$ ), small physical dimensions and low flight speeds. These characteristics can result in degraded aerodynamic performance, intrinsically unsteady flight characteristics and sensitivity to the flight environments. The low Reynolds number flow regime was also characterized by low lift-to-drag ratio with problems of lift generation and flow attachment (Lissaman, 1983). However, it is required that these MAVs must have excellent aerodynamic efficiency and can adapt to different operating circumstances, such as gusts, ground effects, high angles of attack, variable temperature and density media. The controllability of these MAVs is also expected. Accordingly, promoting the aerodynamic performance of micro air vehicles has gradually become a great challenge.

Biological morphing-wing concept has been found to be important in the design of efficient MAVs, which is mainly because the sizes and operating conditions of MAVs are similar as natural flyers. The flexible membrane wings of bats were identified to be one of the essential features causing the aerodynamic superiority in maneuvering (Swartz et al. 2012). Considering the additional advantages of the membrane wings on reduced weight, high impact resistance and easier foldability (Bleischwitz 2016), it is worthwhile to investigate the aerodynamics of the membrane wings and their potential applications on MAVs.

Numerous works focused on membrane wings have been carried out in the past two decades. In the pioneering studies, Levin and Shyy (2001) attached a flexible membrane on the upper surface of a modified CLARK-Y airfoil and found the aerodynamic performance of the airfoil was improved with

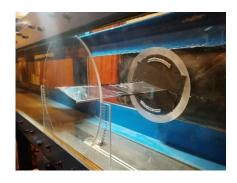
such a passive control approach. Membrane wings were further observed to have unique advantages on delaying stall and adapting to the unsteady flight environment with the introduction in MAVs for sustained, robust and stable flight performance (Shyy et al. 2005). Subsequently, a fine pterosaur-like elasto-flexible morphing wing configuration was proposed and manufactured by Béguin et al. (2012). Flexible membranes were also used in their studies as aerodynamic surfaces for various planform geometries and airfoil shapes. It was shown that the passive membrane deflection combined with the active wing planform variation could effectively maintain high lift-to-drag ratios over a broad range of flight conditions. These studies mainly focused on applying flexible membrane wings on relatively complex configurations of MAVs, remaining the fundamental physical mechanisms to be solved.

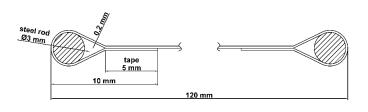
Consequently, simplified membrane wings composed of a rigid support and a flexible wing surface were designed for fundamental research. Generally, there are three most common configurations of membrane wings in the literature: perimeter supported (Albertani et al. 2007; Rojratsirikul et al. 2011; Bleischwitz et al. 2016, 2017, 2018), batten supported (Albertani et al. 2007; Hu et al. 2008; Timpe et al. 2013) and leading/trailing supported (Galvao et al. 2006; Song et al. 2008; Rojratsirikul et al. 2009, 2010; Bleischwitz et al. 2015). Aerodynamic forces, dynamic characteristics and flow field of these membrane wings were investigated and a preliminary conclusion was drawn. Unlike the conventional rigid wings, membrane wings benefit a lot from their fluid-structure interaction characteristics (Gursul et al. 2014). The structures can passively deform and vibrate under the aerodynamic load, leading to camber changing. While in turn, the forces and the flow field are greatly influenced by the structural variations. However, few experimental studies have clarified the exact relationship between membrane vibration and vortex evolution, which is so-called fluid-structure coupling mechanism. As necessary for this aim, the time-resolved global flow fields as well as the time-synchronized membrane deformations are also rarely measured.

In this paper, a two-dimensional time-resolved (2D-TR) PIV was conducted for exploring the fluid-structure interaction of a membrane wing. The flow field and the membrane deformations were simultaneously captured. The full text is divided into following parts: introduction, experimental method, membrane dynamics, flow field and conclusion.

# 2 Experimental method

The present experiment was carried out in the low-speed, open-loop closed-jet wind tunnel at Beijing University of Aeronautics and Astronautics. The test section of the tunnel has a cross section of 42cm (width) × 50cm (height) with the free-stream turbulent intensity of about 0.3%. As shown in Fig. 1(a), the membrane wing was mounted in the test section through the leading/trailing edge supports and endplates. The tested angle of attack was  $\alpha = 14^\circ$ , which belongs to moderate angle of attack in the previous relevant works. The wing had a span of 360mm and chord length of c = 120mm. The free stream velocities  $U_\infty$  were in the range of 7.5 m/s  $\sim 10$ m/s, resulting in the Reynolds number based on c of  $Re = 6 \times 10^4 \sim 8 \times 10^4$ . The membrane wing illustrated in Fig. 1(b) was similar to the model of Bleischwitz et al. (2015), which was attached around 3mm round steel leading/trailing edges without pre-strain. The membrane was made from a transparent thermoplastic polyurethanes (TPU) sheet with a thickness of t = 0.2mm, Young's modulus of t = 31.2mPa and density of t = 1.1g/cm³. The aeroelastic parameter is  $t = (Et/qc)^{1/3}$ , which in this study had a value of  $t = 15.1 \sim 9.5$  for t = 1.5 of t





- (a) Membrane wing in the test section
- (b) Details of membrane wing

Figure 1: Model installation.

PIV measurement was undertaken at the wing mid-span in a streamwise wing-normal plane. Illumination of the desired plane was achieved by using a Beamtech Vlite Hi-527 high-speed double-pulsed laser with a maximum energy of 30mJ/pulse at 1 kHz frame rate. The thickness of the laser sheet was approximately 1mm. A Photron Fastcam SA2/86K-M3 high-speed CMOS camera was placed normal to the flow to capture image pairs. The laser and the camera were synchronized by a MicroVec Micropulse 725 synchronizer. The sampling speed was set to 1 kHz at a spatial resolution of  $1024 \times 800$  pixels, producing sequences of 14000 instantaneous velocity fields over 14 seconds. Glycerol-water mixture droplets with a mean size of about  $1\mu\text{m}$  were generated and seeded by an AG 1500W fog machine as tracer particles. The raw images were processed based on the multi-pass iterative Lucas-Kanade algorithm (MILK) accelerated by GPU (Pan et al. 2015) to obtain original velocity fields. The interrogation window size was set to  $32 \times 32$  pixels with a 75% overlap.

## 3 Membrane dynamics

The dynamic characteristics of the membrane wing which could be extracted from the membrane deformations were firstly analyzed. The mean and instantaneous membrane profiles at  $\alpha = 14^{\circ}$  are shown in Fig. 2(a), (b) and (c). The standard deviations of the vertical membrane motions  $z_{std}$  (see Eq. 1) are presented in Fig. 2(d). It can be observed that the first-order, second-order and third-order modes are dominant vibration modes at each Re respectively. The mode number of the membrane wing increases with Re, which is consistent with previous observations of Rojratsirikul et al. (2009). It is also found in Fig. 2 that the maximum camber of the membrane wing slightly increases with Re. This is because the increasing Re leads to the increase of pressure difference between the upper and lower wing surfaces and thus causes greater membrane deformation.

$$z_{std}(x,y) = \sqrt{\frac{1}{T} \sum_{t=0}^{T} (z(x,y,t) - \bar{z}(x,y))^2}$$
 (1)

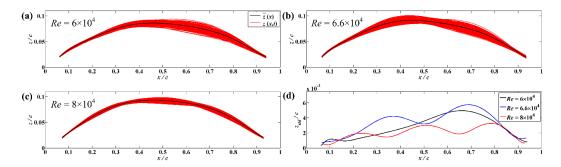


Figure 2: Membrane dynamics. (a)  $Re = 6 \times 10^4$ ; (b)  $Re = 6.6 \times 10^4$ ; (c)  $Re = 8 \times 10^4$ ; (d) Standard deviations of the vertical membrane motions.

## 4 Flow field

As for the flow field, the statistical characteristics were investigated. Normalized time-averaged velocity ( $\sqrt{U^2+V^2}/U_\infty$ ) as well as the time-averaged streamlines are shown in Fig. 3(a). It can be seen that there exists a recirculation region over the membrane wing surface near the trailing edge at  $Re=6\times10^4$ , where the membrane presents a first-order-dominant vibration mode. The size of the recirculation region greatly decreases and basically disappears at  $Re=6.6\times10^4$ , where the membrane presents a second-order-dominant vibration mode. However, a recirculation region appears downstream the trailing edge at  $Re=8\times10^4$ , where the membrane presents a third-order-dominant vibration mode. The differences of the size and position of recirculation region among these Re cases may result from the fluid-structure interaction. Fig. 3(b) shows the normalized time-averaged vorticity ( $\omega c/U_\infty$ ). The negative and positive value regions indicate the shear layers of the leading edge and trailing edge, respectively. With the increase of Re, the shear layer at the wing leeward side shows a tendency to approach the membrane wing surface.

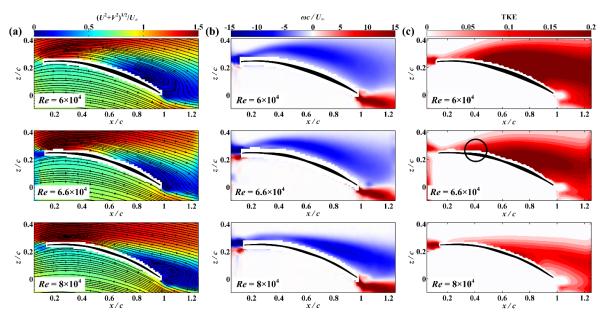


Figure 3: Membrane dynamics. (a) Time averaged velocity and streamlines; (b) Time averaged vorticity; (c) Turbulent kinetic energy.

Moreover, the normalized turbulent kinetic energy  $(\overline{u'^2+v'^2}/U_\infty^2)$ , TKE, is presented in Fig. 3(c). Membrane wings are found to exhibit strong velocity fluctuations over the wing surface and very weak velocity fluctuations below the wing surface. Similarly, the tendency of the shear layer to approach the wing surface with Re increasing can be discovered. Besides, comparing with  $Re = 6 \times 10^4$  case, there seems to be another TKE concentrated region at a more upstream position at  $Re = 6.6 \times 10^4$  (marked with the black circle). Considering the second-order-dominant vibration mode at this Re, it can be deduced that the membrane vibration and the velocity fluctuations have a close relationship due to the fluid-structure interaction.

Frequency characteristics of the time-resolved flow fields and membrane motions were further studied. The vibration of the membrane wing as well as the flow field were found to be quasi-periodic. Hence, Fourier mode decomposition (FMD) (Ma et al. 2015) was adopted to analyze the relationship between the membrane wing and the flow. The frequency spectra of the global flow field and membrane are plotted in Figure 4. It is clear that the membrane vibrations present obvious dominant frequency peaks in all *Re* cases. Specifically, 35.1Hz, 69.7Hz and 108Hz for the first–order, second-order and third-order dominant mode cases. 69.7Hz and 108Hz seem to be the double and triple frequencies of 35.1Hz.

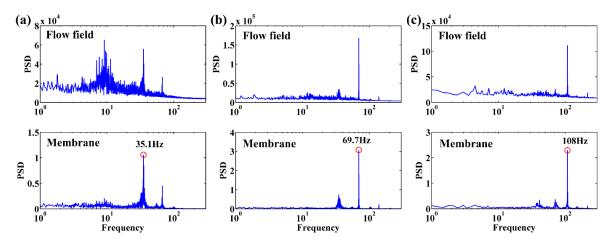


Figure 4: Frequency spectra of the global flow field and membrane. (a)  $Re = 6 \times 10^4$ ; (b)  $Re = 6.6 \times 10^4$ ; (c)  $Re = 8 \times 10^4$ .

The vibration frequencies of the membrane wing are strongly related to the global flow field spectra. In Fig. 4(b) and (c), the global flow field spectra show a similarity with the membrane vibration spectra. They both have identical and obvious dominant frequencies while the lower frequency contributions to the spectra are relatively small. The consistence of the dominant frequency between the global flow field and the membrane wing means the flow and the membrane vibration reach a coupling state. The vibration frequency of the membrane wing is also accurately reflected in the global flow field spectra in Fig. 4(a). However, the dominant frequency of the flow field is located at a much lower frequency around 9Hz. The possible reason for this frequency is the occurrence of vortex merging.

The dynamic Fourier modes corresponding to the membrane vibration frequencies could be obtained by FMD method and are presented in Figure 5. These Fourier modes based on vertical velocities mainly present vortex shedding processes in the shear layer at the wing leeward side. Considering the high contributions of the membrane vibration frequencies in the flow field spectra, the dominant

feature of the flow is the vortex shedding over the wing surface. As shown, the size of the Fourier mode and the distance between adjacent structures gradually reduce with the increase of *Re*. Besides, it should be noticed that the wavelength of membrane vibration also decreases due to the shift of vibration mode with the increase of *Re*. The consistence of the wavelength between the vortex structures and membrane vibration further indicates a fluid-structure coupling state.

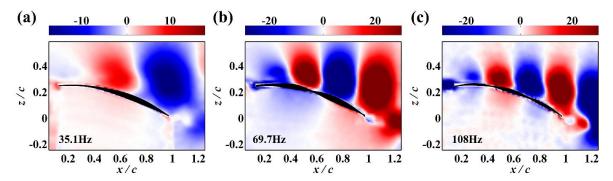


Figure 5: Global Fourier modes based on vertical velocities. (a)  $Re = 6 \times 10^4$ ; (b)  $Re = 6.6 \times 10^4$ ; (c)  $Re = 8 \times 10^4$ .

## 5 Conclusion

This paper experimentally discussed the fluid-structure interaction of a flexible membrane wing at a moderate angle of attack. With the increase of *Re*, the camber of the membrane wing slightly increased while the vibration modes shifted from first-order-dominant mode to third-order-dominant mode. The membrane vibration could enhance the velocity fluctuations over the wing surface, which had a significant influence on the flow field. The dominant frequencies of the flow fields and the vortex shedding processes were greatly changed with the shift of vibration modes due to the fluid-structure interaction.

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